



**W0224-001A  
APOLLO CRADLES LTD  
1.5M X-BEAM 2016  
DESIGN CHECK CALCULATIONS**


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DEC 2016

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CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	Brief			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

**Brief**

The brief is to prepare calculated values for the capacity of the Apollo 1.5m X-Beam to BS EN 1999-1-1.

The beams are manufactured from tube extrusions in aluminium alloy 6082 T6.

**Alloy**

The alloy used is 6082 T6:

For extruded profiles/tubes with thickness less than 5mm:

$$\begin{aligned}
P_{o,haz} &= 0.50 \\
P_{u,haz} &= 0.64 \\
F_o &= 250 \text{ N/mm}^2 \\
F_u &= 290 \text{ N/mm}^2
\end{aligned}$$

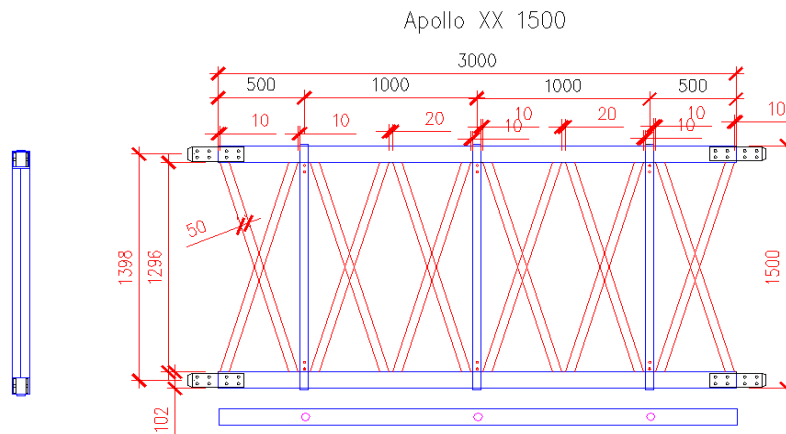
For extruded profiles/tubes with thickness greater than 5mm:

$$\begin{aligned}
P_{o,haz} &= 0.48 \\
P_{u,haz} &= 0.60 \\
F_o &= 260 \text{ N/mm}^2 \\
F_u &= 310 \text{ N/mm}^2
\end{aligned}$$

**Layout**

All beam lengths define the overall length of beam and not the span. As the beam is supported at the verticals, all spans are 1m less than the beam length.

The geometry of the beam is shown in the drawing below:



**Design**

Eurocode 9: Design of Aluminium structures EN 1999-1-1

Alloy used is 6082 T6 throughout


**Design Assumptions**

6082 T6 Aluminium is to be utilised throughout.

X-beam top and bottom booms are to be restrained at 1.00m c/c's.

All loads are to be applied at node locations.

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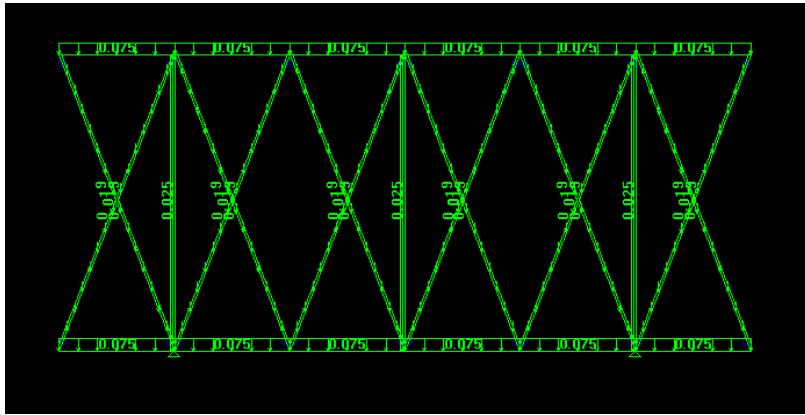
  
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**Load Cases**

Images are shown for a 3m beam, loading for larger beams is applied using the same methodology.

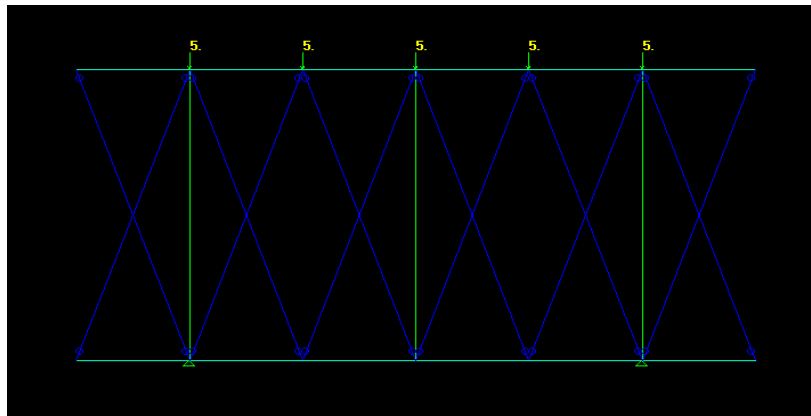
Load Case 1

Self Weight  
 Self weight of all members factored by 1.15 to account for connections



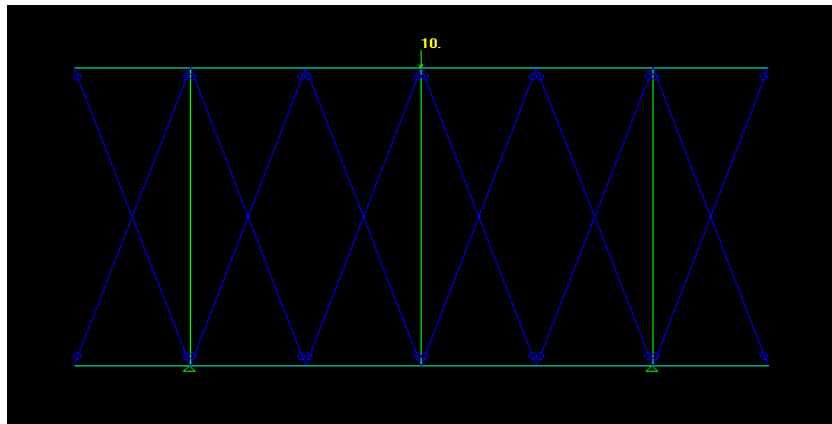
Load Case 2

UDL  
 10kN/m Load Applied to top boom over full length of the X-Beam at node points



Load Case 3

Central Point Load  
 10kN Point Load Applied to Centre of Top Boom of the X-Beam



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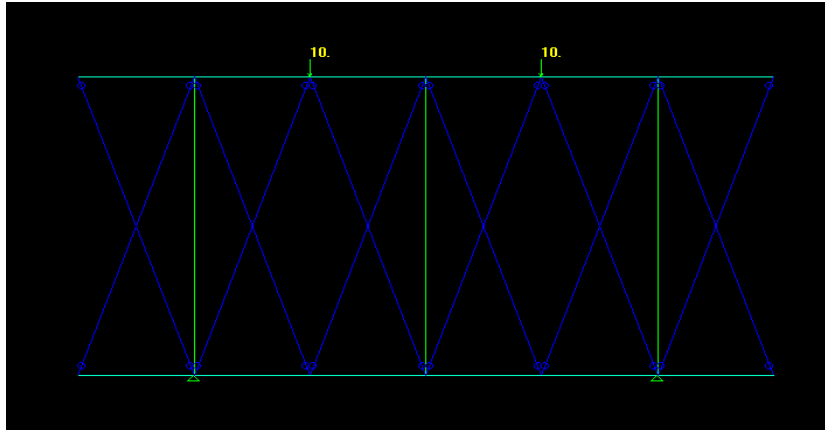


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Load Case 4

Two Point Loads

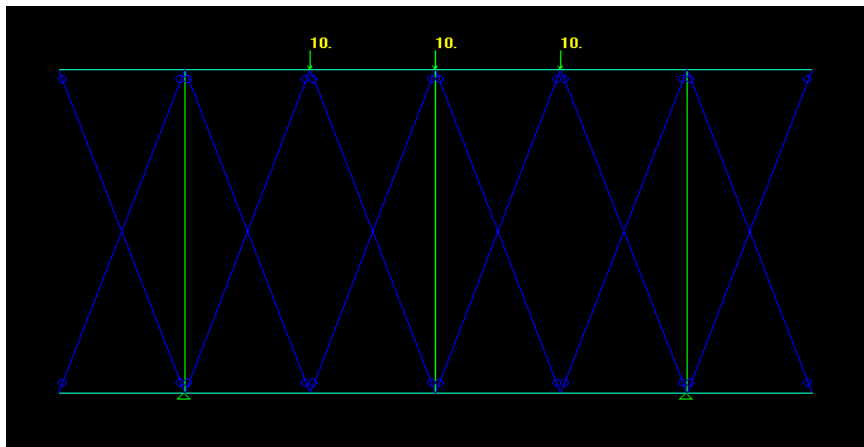
2No 10kN point loads applied at third points along the top boom of the X-Beam.



Load Case 5

Three Point Loads

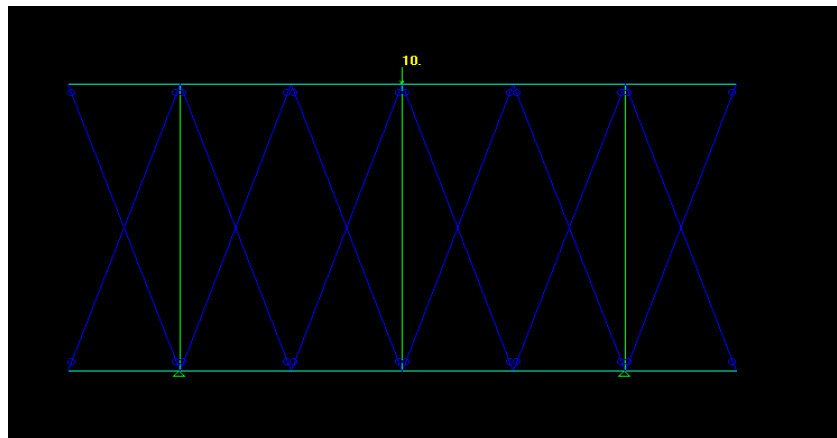
3No 10kN Point Loads applied at quarter points along the X-Beam



Load Case 6

End Shear

10kN Point Load applied 1.0m from support



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### Load Combinations

Combination Number	Combination Description	Load Cases
1	UDL	1+2
2	Central Point Load	1+3
3	Two Point Loads	1+4
4	Three Point Loads	1+5
5	End Shear	1+6

Above Combinations were checked for the following design factors:

$$\gamma_D = 1.35$$

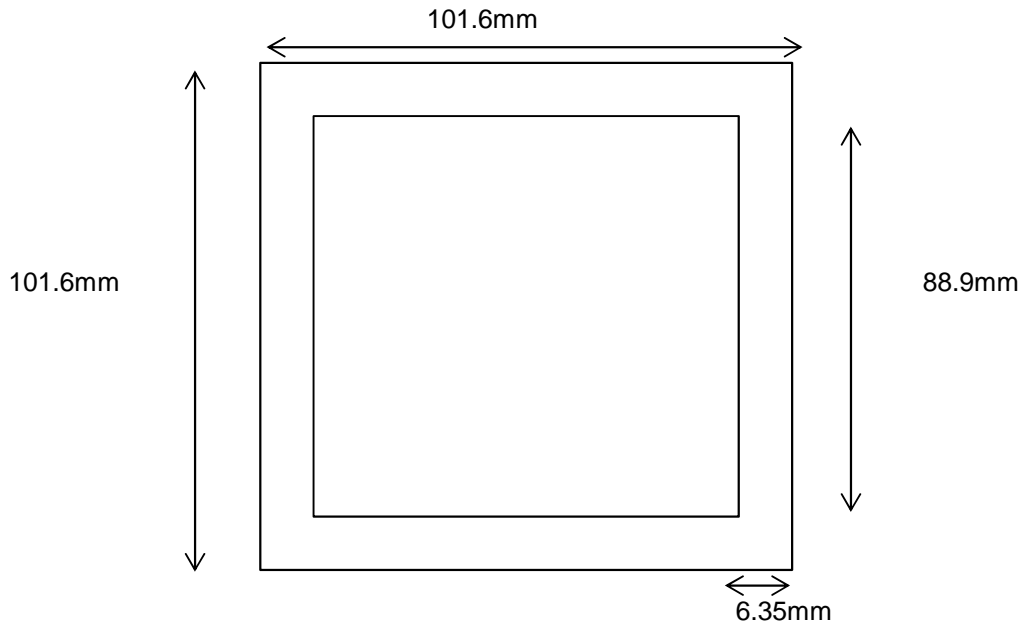
$$\gamma_L = 1.50$$

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	Element :	Main Boom Capacity			
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**Main Boom Capacity**

101.6 x 101.6 x 6.35mm SHS 6082-T2


Alu. 6082-T2	$P_{o,haz} =$	0.48	(Table 3.2b)
	$P_{u,haz} =$	0.60	
	$f_o =$	260 N/mm <sup>2</sup>	
	$f_u =$	310 N/mm <sup>2</sup>	



A=	2419 mm <sup>2</sup>
I=	3674543 mm <sup>4</sup>
$W_{el} =$	72334 mm <sup>3</sup>
$W_{pl} =$	86800 mm <sup>3</sup>
$r_y =$	38.97 mm

for slenderness	$\beta =$	b/t	b=	101.60 mm
	=	16.00	t =	6.35 mm
	$\epsilon =$	sqrt(250/ $f_o$ )	$f_o =$	260 N/mm <sup>2</sup>
	=	0.98		

Class A, without welds, Internal parts	$\beta_1 =$	11 $\epsilon$
	=	11*0.98
	=	10.78
	<	16.00
	$\beta_2 =$	16 $\epsilon$
	=	16*0.98
	=	15.68
	<	16.00

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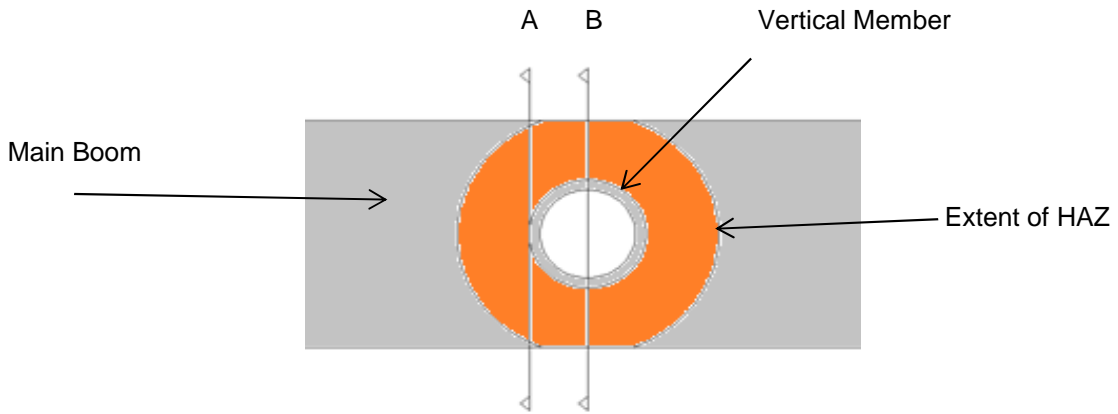
$$\begin{aligned}
\beta_3 &= 22\varepsilon \\
&= 22 \times 0.98 \\
&= 21.56 \\
&> 16.00
\end{aligned}$$

Section is class 3

**Main Boom HAZ**

There are HAZ's at welded joints to the diagonal and vertical.  
HAZ Section at diagonal not considered as Vertical HAZ is more detrimental

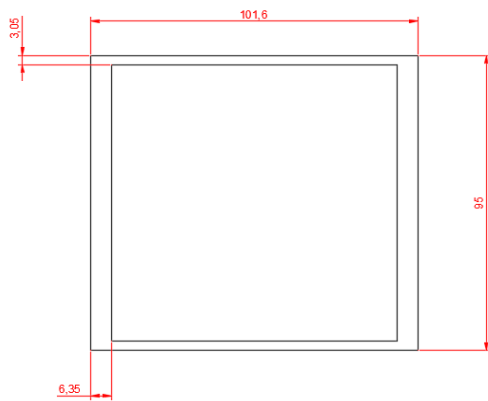
Two HAZ sections considered at the vertical, one at the edge of the vertical (A-A) and one through the mid-section of the vertical (B-B).



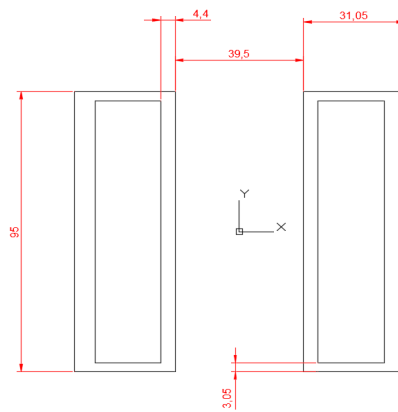
**PLAN VIEW OF VERTICAL TO MAIN BOOM CONNECTION**

Take sections shown below as heat affected

**SHS P<sub>o,haz</sub> HAZ Section Layout**




Section A-A



Section B-B

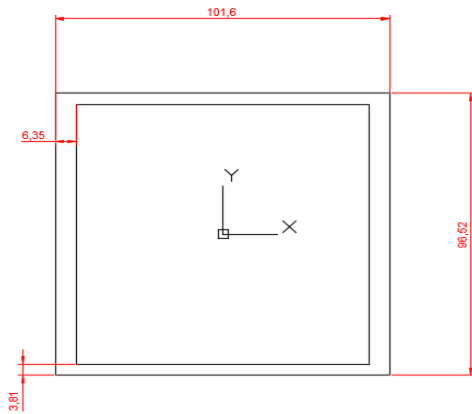


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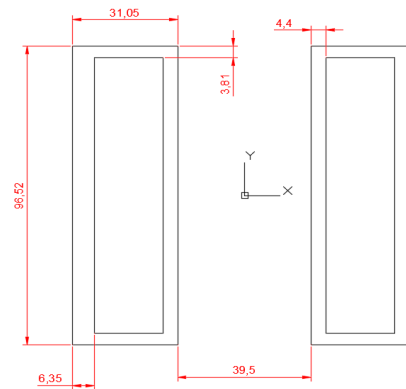
	<u>A-A</u>	<u>B-B</u>	
A=	<b>1748.0</b>	2290.2	mm <sup>2</sup>
I=	<b>3097368.8</b>	3444575.0	mm <sup>4</sup>
W <sub>el,PoHAZ</sub> =	<b>65207.8</b>	72517.4	mm <sup>3</sup>
W <sub>pl,PoHAZ</sub> =	<b>78249.3</b>	87020.8	mm <sup>3</sup>
r <sub>y</sub> =	<b>42.1</b>	38.8	mm

Conservatively, use section A-A as HAZ section properties are lower.

### SHS P<sub>u,haz</sub> HAZ Section Layout



Section A-A



Section B-B

	<u>A-A</u>	<u>B-B</u>	
A=	<b>1903.0</b>	2384.6	mm <sup>2</sup>
I=	<b>3230562.0</b>	3569613.0	mm <sup>4</sup>
W <sub>el,PuHAZ</sub> =	<b>66940.8</b>	73966.3	mm <sup>3</sup>
W <sub>pl,PuHAZ</sub> =	<b>80328.9</b>	88759.5	mm <sup>3</sup>
r <sub>y</sub> =	<b>41.2</b>	38.7	mm

Conservatively, use section A-A as HAZ section properties are lower.

### Boom SHS Moment Capacity

(6.2.5.1)

Non-HAZ

$$M_{o,Rd} = \alpha W_{el} f_o / \gamma_{M1}$$

$$\alpha_{3,u} = 1.00 \text{ (Table 6.4)}$$


$$W_{el} = 72.33 \text{ cm}^3$$

$$f_o = 260 \text{ N/mm}^2$$

$$\gamma_{M1} = 1.1 \text{ (6.1.3)}$$

$$= 1.00 * 72.33 * 260 / 1100$$

$$M_{o,Rd} = 17.10 \text{ kNm}$$

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HAZ

$$M_{u,Rd} = W_{net} f_u / \gamma_{M2}$$

$$W_{net} = W_{el,PuHAZ}$$

$$= 66.94 \text{ cm}^3$$

$$f_u = 310 \text{ N/mm}^2$$

$$\gamma_{M2} = 1.25 (6.1.3)$$

$$= 66.94 * 310 / 1250$$

$$M_{u,Rd} = 16.60 \text{ kNm}$$

$$M_{Rd,x} = 16.60 \text{ kNm} \quad \text{lesser value of } M_{c,Rd} / M_{u,Rd}$$

**Boom SHS Shear Capacity**

(6.2.6)

$$V_{Rd} = A_v f_o / \sqrt{3} \gamma_{M1}$$

$$A_v = 0.6 A_e$$

$$A_v = 0.6 * 1748$$


$$A_v = 1,048.80 \text{ mm}^2$$

$$\gamma_{M1} = 1.1$$

$$f_o = 260 \text{ N/mm}^2$$

$$= 1048.80 * 260 / (\text{SQRT}(3) * 1100)$$

$$V_{Rd} = 143.12 \text{ kN}$$

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### Boom SHS Axial Comp Capacity @ 1000mm (effective length of beam between restraints)

Without Weld  $N_{b,Rd} = kX\omega_x A_{eff} f_o / \gamma_{M1}$  (6.3.1.1 (6.49a))

$$N_{cr} = \pi^2 EI / k^2 L^2 \quad (\text{Appendix I.3})$$

$$E = 70,000 \text{ N/mm}^2$$

$$I = 3,674,543 \text{ mm}^4$$

$$k = 0.50$$

$$L = 1,000 \text{ mm}$$

$$N_{cr} = ((\pi)^2 * 70000 * 3674543) / ((0.5^2) * (1000^2))$$

$$= 10,154,560.01 \text{ N}$$

$$\lambda = \sqrt{A_{eff} f_o / N_{cr}} \quad (6.3.1.2)$$

$$= 0.25$$

$$A_{eff} = 2419 \text{ mm}^2$$

$$A = 2,419 \text{ mm}^2$$

$$X = 1 / \Phi + \sqrt{\Phi^2 - \lambda^2}$$

$$\Phi = 0.5(1 + \alpha(\lambda - \lambda_o) + \lambda^2)$$

$$\alpha = 0.20 \text{ Table 6.6}$$

$$\lambda_o = 0.10 \text{ Table 6.6}$$

$$\Phi = 0.55$$

$$X = 0.92$$


$$k = 1.00 \quad (\text{no welds})$$

$$\omega_x = 1 / (X + (1 - X) \sin(\pi) x_s / l_{cr})$$

$$= 1.08$$

$$N_{b,Rd} = 1.00 * 0.92 * 1.08 * 2419 * 260 / 1100$$

$$= 568.10 \text{ kN}$$

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Localised Weld

$$N_{b,Rd} = X_{haz} \omega_{x,haz} A_{u,eff} f_u / \gamma_{M2} \quad (6.3.1.1 \text{ (6.49b)})$$

$$N_{cr} = \pi^2 EI / k^2 L^2 \quad (\text{Appendix I.3})$$

$$E = 70,000 \text{ N/mm}^2$$

$$I = 3,674,543 \text{ mm}^4$$

$$k = 0.50$$

$$L = 1,000 \text{ mm}$$

$$N_{cr} = ((\pi)^2 * 70000 * 3674543) / ((0.5^2) * (1000^2))$$

$$= 10,154,560.01 \text{ N}$$

$$\lambda_{haz} = \sqrt{A_{u,eff} f_u / N_{cr}} \quad (6.3.1.2)$$

$$= 0.23$$

$$A_{u,eff} = 1903 \text{ mm}^2$$

$$A = 2,419 \text{ mm}^2$$

$$X = 1 / (\Phi + \sqrt{\Phi^2 - \lambda^2})$$

$$\Phi = 0.5(1 + \alpha(\lambda - \lambda_0) + \lambda^2)$$

$$\alpha = 0.20 \text{ Table 6.6}$$

$$\lambda_0 = 0.10 \text{ Table 6.6}$$

$$\Phi = 0.54$$

$$X = 0.94$$


$$\omega_{x,haz} = 1 / (X_{haz} + (1 - X_{haz}) \sin(\pi) x_{s,haz} / l_{cr})$$

$$= 1.06$$

$$N_{b,Rd} = 0.94 * 1.06 * 1903 * 310 / 1250$$

$$= 470.25 \text{ kN}$$

$$\text{Lesser Value} = 470.25 \text{ kN}$$

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### SHS Axial Tension Capacity

(6.2.3)

#### 1. General yielding

$$N_{o,Rd} = A_g f_o / \gamma_{M1}$$

$f_o =$	260 N/mm <sup>2</sup>
$A_g =$	A
$=$	2419 mm <sup>2</sup>
$\gamma_{M1} =$	1.1

$$= 2419 * 260 / 1100$$

$$= 571.76 \text{ kN}$$

#### 2. Local failure


$$N_{u,Rd} = A_{u,eff} f_u / \gamma_{M2}$$

$f_u =$	310 N/mm <sup>2</sup>
$A_{u,eff} =$	1903 mm <sup>2</sup>
$\gamma_{M1} =$	1.25

$$= 1903 * 310 / 1250$$

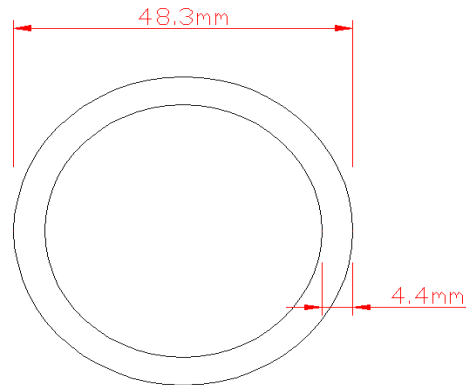
$$= 471.94 \text{ kN}$$

Lesser Value= 471.94 kN

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	Vertical CHS Member Capacity			
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**Vertical CHS Member Capacity**  
ø48.3mm x 4.4mm CHS 6082-T6

Alu. 6082-T2	$P_{o,haz} =$	0.50	(Table 3.2b)
	$P_{u,haz} =$	0.64	
	$f_o =$	250 N/mm <sup>2</sup>	
	$f_u =$	290 N/mm <sup>2</sup>	



**Section Properties**

A=	607 mm <sup>2</sup>
I=	147654 mm <sup>4</sup>
$W_{el} =$	6114 mm <sup>3</sup>
$W_{pl} =$	8254 mm <sup>3</sup>
$r_y =$	15.6 mm

for slenderness	$\beta =$	$b/t$	$b =$	48.3 mm
	$=$	10.98	$t =$	4.4 mm
	$\epsilon =$	$\sqrt{250/f_o}$	$f_o =$	250 N/mm <sup>2</sup>
	$=$	1.00		

Class A, without welds, Internal parts	$\beta_1 =$	11 $\epsilon$
	$=$	11*1.0
	$=$	11.00
	$>$	10.98

Section is class 1

**Vertical CHS HAZ Length**

Full perimeter weld at the joint, therefore the entire section is affected by HAZ.

As per BS EN 1999-1-1, for HAZ wall thickness factored by 0.50 (For  $P_{o,haz}$ )

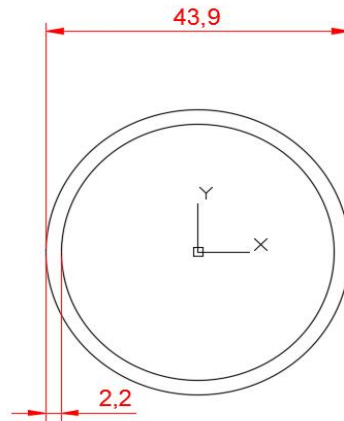
As per BS EN 1999-1-1, for HAZ wall thickness factored by 0.64 (For  $P_{u,haz}$ )

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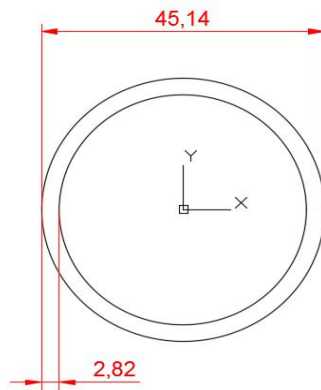
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**Vertical CHS P<sub>o,haz</sub> HAZ Section Layout**




$A_{\text{haz}} =$	288 mm <sup>2</sup>
$I =$	62820 mm <sup>4</sup>
$I_z =$	62820 mm <sup>4</sup>
$W_{\text{el,PoHAZ}} =$	2,862 mm <sup>3</sup>
$W_{\text{pl,PoHAZ}} =$	3,864 mm <sup>3</sup>

**Vertical CHS P<sub>u,haz</sub> HAZ Section Layout**



$A_{\text{haz}} =$	374 mm <sup>2</sup>
$I =$	84308 mm <sup>4</sup>
$I_z =$	84308 mm <sup>4</sup>
$W_{\text{el,PuHAZ}} =$	3,735 mm <sup>3</sup>
$W_{\text{pl,PuHAZ}} =$	5,043 mm <sup>3</sup>

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### Vertical CHS Moment Capacity

(6.2.5.1)

Non-HAZ

$$M_{o,Rd} = \alpha W_{el} f_o / \gamma_{M1}$$

$$\alpha = W_{pl}/W_{el} \text{ (Table 6.4)}$$

$$= 1.35$$

$$W_{el} = 6.11 \text{ cm}^3$$

$$f_o = 250 \text{ N/mm}^2$$

$$\gamma_{M1} = 1.1 \text{ (6.1.3)}$$

$$= 1.35 * 6.11 * 250 / 1100$$

$$M_{o,Rd} = 1.87 \text{ kNm}$$

HAZ

$$M_{u,Rd} = W_{net} f_u / \gamma_{M2}$$

$$W_{net} = W_{el,PuHAZ}$$

$$= 3.74 \text{ cm}^3$$

$$f_u = 290 \text{ N/mm}^2$$

$$\gamma_{M2} = 1.25 \text{ (6.1.3)}$$

$$= 3.74 * 290 / 1250$$

$$M_{u,Rd} = 0.87 \text{ kNm}$$

$$M_{Rd,x} = 0.87 \text{ kNm}$$

lesser value of  $M_{c,Rd} / M_{u,Rd}$

### Vertical CHS Shear Capacity

(6.2.6)

$$V_{Rd} = A_v f_o / \sqrt{3} \gamma_{M1}$$

$$A_v = 0.6 A_e$$

$$A_v = 0.6 * 288$$

$$A_v = 172.80 \text{ mm}^2$$


$$\gamma_{M1} = 1.1$$

$$f_o = 250 \text{ N/mm}^2$$

$$= 172.80 * 250 / (\text{SQRT}(3) * 1100)$$

$$V_{Rd} = 22.67 \text{ kN}$$



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### Vertical CHS Axial Comp Capacity @ 1297mm (effective length of beam)

Without Weld  $N_{b,Rd} = kX\omega_x A_{eff} f_o / \gamma_{M1}$  (6.3.1.1 (6.49a))

$$N_{cr} = \pi^2 EI / k^2 L^2 \quad (\text{Appendix I.3})$$

$$E = 70,000 \text{ N/mm}^2$$

$$I = 147,654 \text{ mm}^4$$

$$k = 0.50$$

$$L = 1,297 \text{ mm}$$

$$N_{cr} = ((\pi)^2 * 70000 * 147654) / ((0.5^2) * (1297^2))$$

$$= 242,562.15 \text{ N}$$

$$\lambda = \sqrt{A_{eff} f_o / N_{cr}} \quad (6.3.1.2)$$

$$= 0.79$$

$$A_{eff} = 607 \text{ mm}^2$$

$$A = 607 \text{ mm}^2$$

$$X = 1 / (\Phi + \sqrt{\Phi^2 - \lambda^2})$$

$$\Phi = 0.5(1 + \alpha(\lambda - \lambda_o) + \lambda^2)$$

$$\alpha = 0.20 \text{ Table 6.6}$$

$$\lambda_o = 0.10 \text{ Table 6.6}$$

$$\Phi = 0.88$$

$$X = 0.57$$


$$k = 1.00 \quad (\text{no welds})$$

$$\omega_x = 1 / (X + (1-X)\sin(\pi(x_s/lcr)))$$

$$= 1.69$$

$$N_{b,Rd} = 1.00 * 0.57 * 1.69 * 607 * 250 / 1100$$

$$= 132.89 \text{ kN}$$

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Localised Weld

$$N_{b,Rd} = X_{haz} \omega_{x,haz} A_{u,eff} f_u / \gamma_{M2} \quad (6.3.1.1 \text{ (6.49b)})$$

$$N_{cr} = \pi^2 EI / k^2 L^2 \quad (\text{Appendix I.3})$$

$$E = 70,000 \text{ N/mm}^2$$

$$I = 147,654 \text{ mm}^4$$

$$k = 0.50$$

$$L = 1,297 \text{ mm}$$

$$N_{cr} = ((\pi)^2 * 70000 * 147654) / ((0.5^2) * (1297^2))$$

$$= 242,562.15 \text{ N}$$

$$\lambda_{haz} = \sqrt{A_{u,eff} f_u / N_{cr}} \quad (6.3.1.2)$$

$$= 0.63$$

$$A_{u,eff} = 374 \text{ mm}^2$$

$$A = 607 \text{ mm}^2$$

$$X = 1 / (\Phi + \sqrt{\Phi^2 - \lambda^2})$$

$$\Phi = 0.5(1 + \alpha(\lambda - \lambda_0) + \lambda^2)$$

$$\alpha = 0.20 \text{ Table 6.6}$$

$$\lambda_0 = 0.10 \text{ Table 6.6}$$

$$\Phi = 0.75$$

$$X = 0.67$$


$$\omega_{x,haz} = 1 / (X_{haz} + (1 - X_{haz}) \sin(\pi) x_{s,haz} / l_{cr})$$

$$= 1.45$$

$$N_{b,Rd} = 0.67 * 1.45 * 374 * 290 / 1250$$

$$= 84.30 \text{ kN}$$

$$\text{Lesser Value} = 84.30 \text{ kN}$$

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	Vertical CHS Member Capacity			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

### Vertical CHS Axial Tension Capacity

(6.2.3)

#### 1. General yielding

$$N_{o,Rd} = \frac{A_g f_o}{\gamma_{M1}}$$

$f_o =$	250 N/mm <sup>2</sup>
$A_g =$	A
$=$	607 mm <sup>2</sup>
$\gamma_{M1} =$	1.1

$$= \frac{607 \times 250}{1100}$$

$$= 137.95 \text{ kN}$$

#### 2. Local failure


$$N_{u,Rd} = \frac{A_{u,eff} f_u}{\gamma_{M2}}$$

$f_u =$	290 N/mm <sup>2</sup>
$A_{u,eff} =$	374 mm <sup>2</sup>
$\gamma_{M1} =$	1.25

$$= \frac{374 \times 290}{1250}$$

$$= 86.77 \text{ kN}$$

Lesser Value= 86.77 kN

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	SHS Diagonal Capacity			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

### SHS Diagonal Layout

50.8 x 50.8 x 3mm SHS 6082-T2

Alu. 6082-T2

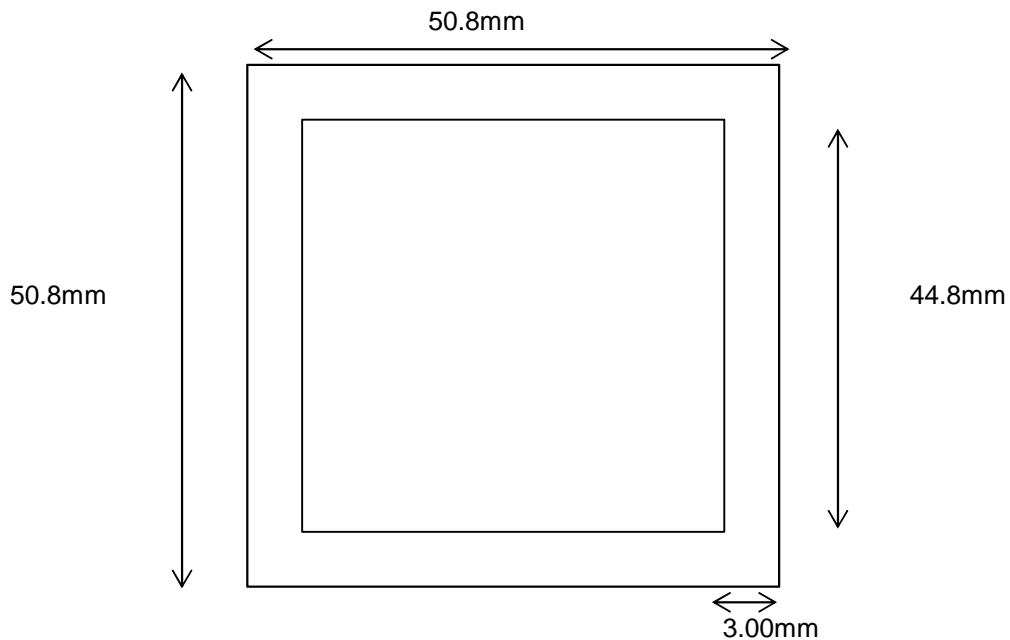
$$P_{o,haz} = 0.50$$

(Table 3.2b)

$$P_{u,haz} = 0.64$$

$$f_o = 250 \text{ N/mm}^2$$

$$f_u = 290 \text{ N/mm}^2$$



$$A = 574 \text{ mm}^2$$

$$I = 219291 \text{ mm}^4$$

$$W_{el} = 8634 \text{ mm}^3$$

$$W_{pl} = 10360 \text{ mm}^3$$

$$r_y = 19.55 \text{ mm}$$

for slenderness

$$\beta = b/t \quad b = 50.80 \text{ mm}$$

$$= 16.93 \quad t = 3.00 \text{ mm}$$

$$\varepsilon = \sqrt{250/f_o} \quad f_o = 250 \text{ N/mm}^2$$

$$= 1.00$$

Class A, without welds, Internal parts

$$\beta_1 = 11\varepsilon$$

$$= 11 \cdot 1.00$$

$$= 11.00$$


$$< 16.93$$

$$\beta_2 = 16\varepsilon$$

$$= 16 \cdot 1.00$$

$$= 16.00$$

$$< 16.93$$

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	SHS Diagonal Capacity			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

$$\begin{aligned}
\beta_3 &= 22\varepsilon \\
&= 22 * 1.00 \\
&= 22.00 \\
&> 16.93
\end{aligned}$$

Section is class 3

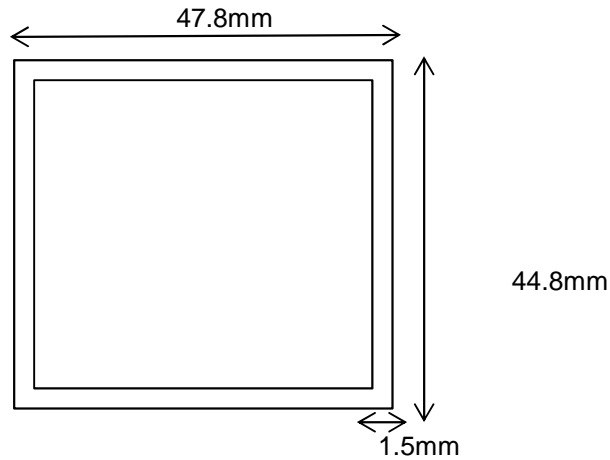
### SHS Diagonal HAZ Length

Full perimeter weld at the joint, therefore the entire section is affected by HAZ.


As per BS EN 1999-1-1, for HAZ wall thickness factored by 0.50 (For  $P_{o,haz}$ )

As per BS EN 1999-1-1, for HAZ wall thickness factored by 0.64 (For  $P_{u,haz}$ )

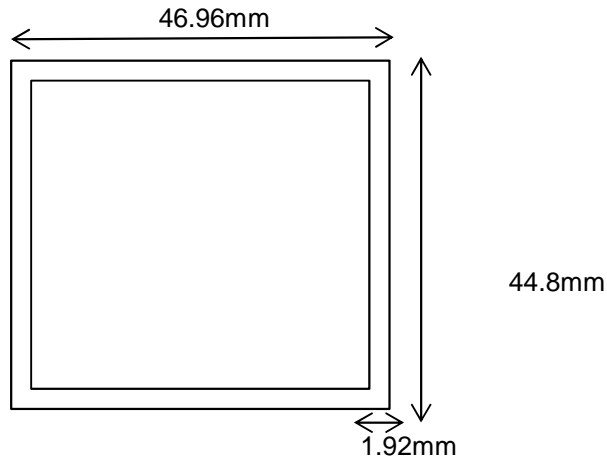
### SHS Diagonal $P_{o,haz}$ HAZ Section Layout



$$\begin{aligned}
A_{haz} &= 278 \text{ mm}^2 \\
I &= 99357 \text{ mm}^4 \\
I_z &= 99357 \text{ mm}^4 \\
W_{el,PoHAZ} &= 4,157 \text{ mm}^3 \\
W_{pl,PoHAZ} &= 4,989 \text{ mm}^3
\end{aligned}$$

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	SHS Diagonal Capacity			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

### SHS Diagonal $P_{u,haz}$ HAZ Section Layout



$$\begin{aligned}
A_{haz} &= 358 \text{ mm}^2 \\
I_x &= 130752 \text{ mm}^4 \\
I_z &= 130752 \text{ mm}^4 \\
W_{el,PuHAZ} &= 5,376 \text{ mm}^3 \\
W_{pl,PuHAZ} &= 6,452 \text{ mm}^3
\end{aligned}$$

### SHS Diagonal Axial Tension Capacity


(6.2.3)

#### 1. General yielding

$$\begin{aligned}
N_{o,Rd} &= A_g f_o / \gamma_{M1} \\
f_o &= 250 \text{ N/mm}^2 \\
A_g &= A \\
&= 574 \text{ mm}^2 \\
\gamma_{M1} &= 1.1 \\
&= 574 * 250 / 1100 \\
&= 130.45 \text{ kN}
\end{aligned}$$

#### 2. Local failure

$$\begin{aligned}
N_{u,Rd} &= A_{u,eff} f_u / \gamma_{M2} \\
f_u &= 290 \text{ N/mm}^2 \\
A_{u,eff} &= 358 \text{ mm}^2 \\
\gamma_{M1} &= 1.25 \\
&= 358 * 290 / 1250 \\
&= 83.06 \text{ kN} \\
\text{Lesser Value} &= 83.06 \text{ kN}
\end{aligned}$$

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	SHS Diagonal Capacity			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

### SHS Diagonal Axial Comp Capacity @ 732mm (effective length of beam)

Without Weld  $N_{b,Rd} = kX\omega_x A_{eff} f_o / \gamma_{M1}$  (6.3.1.1 (6.49a))

$$N_{cr} = \pi^2 EI / k^2 L^2 \quad (\text{Appendix I.3})$$

$$E = 70,000 \text{ N/mm}^2$$

$$I = 219,291 \text{ mm}^4$$

$$k = 0.50$$

$$L = 732 \text{ mm}$$

$$N_{cr} = ((\pi)^2 * 70000 * 219291) / ((0.5^2) * (732^2))$$

$$= 1,130,983.90 \text{ N}$$

$$\lambda = \sqrt{A_{eff} f_o / N_{cr}} \quad (6.3.1.2)$$

$$= 0.36$$

$$A_{eff} = 574 \text{ mm}^2$$

$$A = 574 \text{ mm}^2$$

$$X = 1 / \Phi + \sqrt{\Phi^2 - \lambda^2}$$

$$\Phi = 0.5(1 + \alpha(\lambda - \lambda_o) + \lambda^2)$$

$$\alpha = 0.20 \text{ Table 6.6}$$

$$\lambda_o = 0.10 \text{ Table 6.6}$$

$$\Phi = 0.59$$

$$X = 0.86$$


$$k = 1.00 \quad (\text{no welds})$$

$$\omega_x = 1 / (X + (1 - X) \sin(\pi) x_s / l_{cr})$$

$$= 1.16$$

$$N_{b,Rd} = 1.00 * 0.86 * 1.16 * 574 * 250 / 1100$$

$$= 130.14 \text{ kN}$$

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	SHS Diagonal Capacity			
	Job Number :	W0224	By : mrb	Date: Dec 16	
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Localised Weld

$$N_{b,Rd} = X_{haz} \omega_{x,haz} A_{u,eff} f_u / \gamma_{M2} \quad (6.3.1.1 \text{ (6.49b)})$$

$$N_{cr} = \pi^2 EI / k^2 L^2 \quad (\text{Appendix I.3})$$

$$E = 70,000 \text{ N/mm}^2$$

$$I = 219,291 \text{ mm}^4$$

$$k = 0.50$$

$$L = 732 \text{ mm}$$

$$N_{cr} = ((\pi)^2 * 70000 * 219291) / ((0.5^2) * (732^2))$$

$$= 1,130,983.90 \text{ N}$$

$$\lambda_{haz} = \sqrt{A_{u,eff} f_u / N_{cr}} \quad (6.3.1.2)$$

$$= 0.28$$

$$A_{u,eff} = 358 \text{ mm}^2$$

$$A = 574 \text{ mm}^2$$

$$X = 1 / (\Phi + \sqrt{\Phi^2 - \lambda^2})$$

$$\Phi = 0.5(1 + \alpha(\lambda - \lambda_0) + \lambda^2)$$

$$\alpha = 0.20 \text{ Table 6.6}$$

$$\lambda_0 = 0.10 \text{ Table 6.6}$$

$$\Phi = 0.56$$

$$X = 0.90$$

$$\omega_{x,haz} = 1 / (X_{haz} + (1 - X_{haz}) \sin(\pi) x_{s,haz} / l_{cr})$$

$$= 1.10$$

$$N_{b,Rd} = 0.90 * 1.10 * 358 * 290 / 1250$$

$$= 82.23 \text{ kN}$$

$$\text{Lesser Value} = 82.23 \text{ kN}$$




CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	12m X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked: mmr	Date: Dec 16



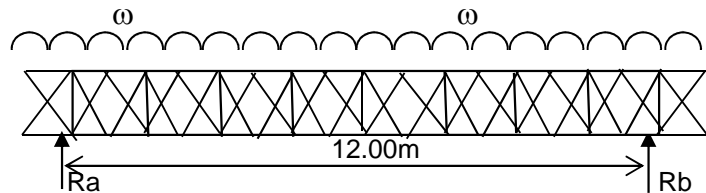
ALAN WHITE DESIGN

# 12m X-Beam Results

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	12m X-Beam Load Combination 1			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 1**      UDL load      10kN/m applied along beam

Element	Action	Formula	Ultimate	Calculated	Factor	
Boom	Moment	$M_{c,Rd}$	16.60	3.72	4.47	
	Shear	$V_{Rd}$	143.12	9.77	14.66	
	Tension	$N_{o,Rd}$	471.94	54.37	8.68	
	Compression	$N_{b,Rd}$	470.25	164.18	2.86	
	Deflection	d		120.00	17.80	6.74
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$			1.00	1.89
Vertical	Moment	$M_{c,Rd}$	0.87	0.13	6.89	
	Shear	$V_{Rd}$	22.67	0.18	128.83	
	Tension	$N_{o,Rd}$	86.77	0.75	115.85	
	Compression	$N_{b,Rd}$	84.30	25.07	3.36	
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$			1.00	2.43
Diagonal	Tension	$N_{o,Rd}$	83.06	38.11	2.18	
	Compression	$N_{b,Rd}$	82.23	49.46	1.66	
<b>Factor</b>					<b>1.66</b>	



$$\text{Max Moment} = WL^2/8$$

so for ultimate condition

$$W = 1.5 \times 10 = 15.00 \text{ kN}$$

apply factor from above

$$Wf = 15 \times 1.66 = 24.90 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= Wf \times 12^2 / 8 \\ &= (24.90 \times 12^2) / 8 \\ &= 448.20 \text{ kNm} \end{aligned}$$

and for allowable value

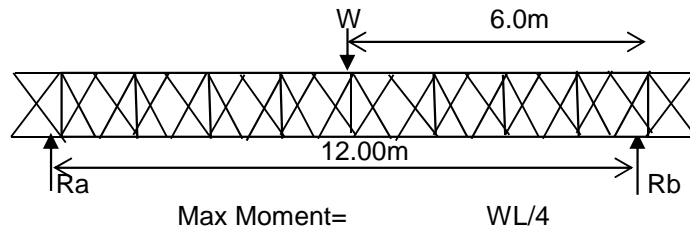
$$\begin{aligned} \text{allowable max moment} &= 448.20 / 1.50 \\ &= 298.80 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>448.20 kNm</b>
	<b>Allowable</b>	<b>298.80 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	12m X-Beam Load Combination 2			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 2**      Point load      10kN load applied at midspan of beam

Element	Action	Formula	Ultimate	Calculated	Factor	
Boom	Moment	$M_{c,Rd}$	16.60	0.80	20.67	
	Shear	$V_{Rd}$	143.12	2.03	70.64	
	Tension	$N_{o,Rd}$	471.94	15.20	31.05	
	Compression	$N_{b,Rd}$	470.25	30.73	15.30	
	Deflection	$d$		120.00	3.34	35.93
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	9.58
Vertical	Moment	$M_{c,Rd}$	0.87	0.02	51.04	
	Shear	$V_{Rd}$	22.67	0.02	985.83	
	Tension	$N_{o,Rd}$	86.77	0.53	165.27	
	Compression	$N_{b,Rd}$	84.30	2.52	33.48	
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	21.94
Diagonal	Tension	$N_{o,Rd}$	83.06	4.99	16.64	
	Compression	$N_{b,Rd}$	82.23	5.90	13.95	
			<b>Factor</b>		<b>9.58</b>	



so for ultimate condition

$$W = 1.50 \times 10 = 15.00 \text{ kN}$$

apply factor from above

$$W_f = 15 \times 9.58 = 143.70 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= W_f \times L/4 \\ &= 143.70 \times 12/4 \\ &= 431.10 \text{ kNm} \end{aligned}$$

and for allowable value

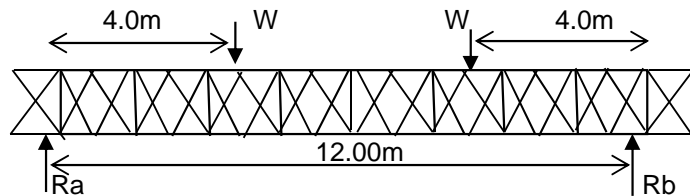
$$\begin{aligned} \text{allowable max moment} &= 431.10/1.50 \\ &= 287.40 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>431.10 kNm</b>
	<b>Allowable</b>	<b>287.40 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	12m X-Beam Load Combination 3			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

**Load Comb. 3**      PL at third points      10kN load applied at each of the two third points

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	0.80	20.73
	Shear	$V_{Rd}$	143.12	2.03	70.57
	Tension	$N_{o,Rd}$	471.94	13.03	36.22
	Compression	$N_{b,Rd}$	470.25	41.21	11.41
	Deflection	d	120.00	4.52	26.55
	Combined Axial	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	7.94
Vertical	Moment	$M_{c,Rd}$	0.87	0.03	27.12
	Shear	$V_{Rd}$	22.67	0.04	539.86
	Tension	$N_{o,Rd}$	86.77	0.63	138.83
	Compression	$N_{b,Rd}$	84.30	4.48	18.80
	Combined Axial	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	12.07
Diagonal	Tension	$N_{o,Rd}$	83.06	9.06	9.17
	Compression	$N_{b,Rd}$	82.23	10.25	8.02
<b>Factor</b>					<b>7.94</b>



$$\text{Max Moment} = WL/3$$

so for ultimate condition

$$W = \frac{1.50 \times 10}{15.00} \text{ kN}$$

apply factor from above

$$W_f = \frac{15.00 \times 7.94}{1} = 119.10 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= W_f \times L / 3 \\ &= (119.10 \times 12) / 3 \\ &= 476.40 \text{ kNm} \end{aligned}$$

and for allowable value

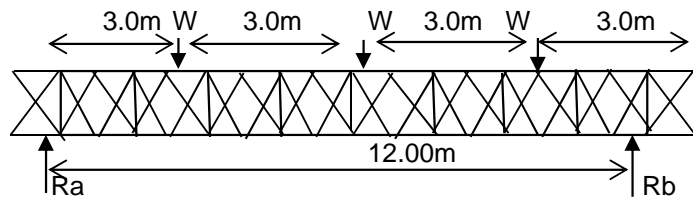
$$\begin{aligned} \text{allowable max moment} &= \frac{476.40}{1.50} \\ &= 317.60 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>476.40 kNm</b>
	<b>Allowable</b>	<b>317.60 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	12m X-Beam Load Combination 4			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

**Load Comb. 4** Load at quarter points  
10kN load applied at each of the three quarter points

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	1.07	15.46
	Shear	$V_{Rd}$	143.12	2.77	51.73
	Tension	$N_{o,Rd}$	471.94	21.12	22.35
	Compression	$N_{b,Rd}$	470.25	57.49	8.18
	Deflection	d	120.00	6.34	18.93
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	5.76
Vertical	Moment	$M_{c,Rd}$	0.87	0.05	18.86
	Shear	$V_{Rd}$	22.67	0.06	365.71
	Tension	$N_{o,Rd}$	86.77	0.73	119.02
	Compression	$N_{b,Rd}$	84.30	6.44	13.08
	Combined Axial	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	8.40
Diagonal	Tension	$N_{o,Rd}$	83.06	13.09	6.34
	Compression	$N_{b,Rd}$	82.23	14.41	5.71
<b>Factor</b>					<b>5.71</b>



$$\text{Max Moment} = WL/2$$

so for ultimate condition

$$W = \frac{1.50 \times 10}{15.00} \text{ kN}$$

apply factor from above

$$W_f = 15.00 \times 5.71 = 85.65 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= W_f \times 12/2 \\ &= (85.65 \times 12)/2 \\ &= 513.90 \text{ kNm} \end{aligned}$$

and for allowable value

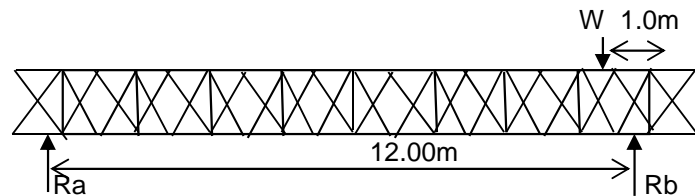
$$\begin{aligned} \text{allowable max moment} &= 513.90/1.50 \\ &= 342.60 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>513.90 kNm</b>
	<b>Allowable</b>	<b>342.60 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	12m X-Beam Load Combination 5			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 5**      End Shear      10kN load applied at a 1.0m distance from the support

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	0.69	23.99
	Shear	$V_{Rd}$	143.12	2.04	70.30
	Tension	$N_{o,Rd}$	471.94	3.76	125.52
	Compression	$N_{b,Rd}$	470.25	11.06	42.51
	Deflection	$d$	120.00	1.08	111.11
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	16.88
Vertical	Moment	$M_{c,Rd}$	0.87	0.01	61.98
	Shear	$V_{Rd}$	22.67	0.02	1133.71
	Tension	$N_{o,Rd}$	86.77	0.24	364.57
	Compression	$N_{b,Rd}$	84.30	4.05	20.81
	Combined Axial	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	16.50
Diagonal	Tension	$N_{o,Rd}$	83.06	6.25	13.29
	Compression	$N_{b,Rd}$	82.23	7.74	10.62
<b>Factor</b>					<b>10.62</b>



$$\text{Max Shear } R_b = W * 11 / 12$$

so for ultimate condition

$$W = \frac{150 * 10}{15.00} \text{ kN}$$

apply factor from above

$$W_f = 15.0 * 10.62 = 159.30 \text{ kN}$$

so maximum shear is as above

$$\begin{aligned} \text{Ultimate } Q_u &= W_f * 11 / 12 \\ &= (159.30 * 11) / 12 \\ &= 146.03 \text{ kN} \end{aligned}$$

and for allowable value

$$\begin{aligned} \text{allowable max shear} &= 146.03 / 1.50 \\ &= 97.35 \text{ kN} \end{aligned}$$

<b>Shear values</b>	<b>Ultimate</b>	<b>146.03 kN</b>
	<b>Allowable</b>	<b>97.35 kN</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	12m X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked: mmr	Date: Dec 16



ALAN WHITE DESIGN

12.0m X-BEAM		
Loadcase	Ultimate	Allowable
No.	Moment	Moment
1 UDL	448.20	298.80
2 Point	431.10	287.40
3 Third	476.40	317.60
4 Quarter	513.90	342.60

Loadcase	Ultimate	Allowable
No.	Shear	Shear
5 End Shear	146.03	97.35

**Max Allowable Moment = 287.40 kNm**

**Max Allowable Shear = 97.00 kN**


CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	18m X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked: mmr	Date: Dec 16



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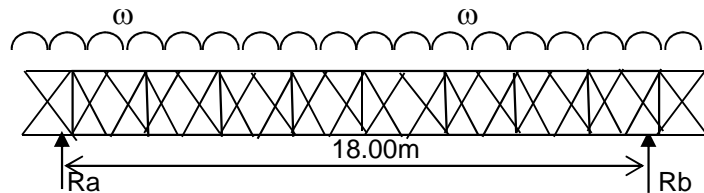
# 18m X-Beam Results



CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	18m X-Beam Load Combination 1			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 1**      UDL load      10kN/m applied along beam

Element	Action	Formula	Ultimate	Calculated	Factor	
Boom	Moment	$M_{c,Rd}$	16.60	5.79	2.87	
	Shear	$V_{Rd}$	143.12	14.93	9.59	
	Tension	$N_{o,Rd}$	471.94	131.02	3.60	
	Compression	$N_{b,Rd}$	470.25	394.20	1.19	
	Deflection	$d$		180.00	73.03	2.46
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	0.90
Vertical	Moment	$M_{c,Rd}$	0.87	0.21	4.13	
	Shear	$V_{Rd}$	22.67	0.29	77.12	
	Tension	$N_{o,Rd}$	86.77	2.67	32.50	
	Compression	$N_{b,Rd}$	84.30	36.68	2.30	
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	1.59
Diagonal	Tension	$N_{o,Rd}$	83.06	62.93	1.32	
	Compression	$N_{b,Rd}$	82.23	76.78	1.07	
			<b>Factor</b>		<b>0.90</b>	



$$\text{Max Moment} = WL^2/8$$

so for ultimate condition

$$W = 1.5 \times 10 = 15.00 \text{ kN}$$

apply factor from above

$$Wf = 15 \times 0.90 = 13.50 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } Mu &= Wf \times 18^2 / 8 \\ &= (13.50 \times 18^2) / 8 \\ &= 546.75 \text{ kNm} \end{aligned}$$

and for allowable value

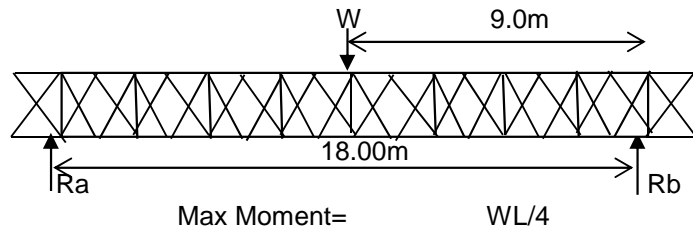
$$\begin{aligned} \text{allowable max moment} &= 546.75 / 1.50 \\ &= 364.50 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>546.75 kNm</b>
	<b>Allowable</b>	<b>364.50 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	18m X-Beam Load Combination 2			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

**Load Comb. 2**      Point load      10kN load applied at midspan of beam

Element	Action	Formula	Ultimate	Calculated	Factor	
Boom	Moment	$M_{c,Rd}$	16.60	0.83	20.00	
	Shear	$V_{Rd}$	143.12	2.00	71.56	
	Tension	$N_{o,Rd}$	471.94	25.01	18.87	
	Compression	$N_{b,Rd}$	470.25	52.07	9.03	
	Deflection	$d$		180.00	9.11	19.76
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	6.67
Vertical	Moment	$M_{c,Rd}$	0.87	0.02	48.20	
	Shear	$V_{Rd}$	22.67	0.03	872.08	
	Tension	$N_{o,Rd}$	86.77	0.40	215.84	
	Compression	$N_{b,Rd}$	84.30	2.74	30.74	
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	20.34
Diagonal	Tension	$N_{o,Rd}$	83.06	5.55	14.97	
	Compression	$N_{b,Rd}$	82.23	6.12	13.44	
<b>Factor</b>					<b>6.67</b>	



so for ultimate condition

$$W = 1.50 \times 10 = 15.00 \text{ kN}$$

apply factor from above

$$W_f = 15 \times 6.67 = 100.05 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= W_f \times 18/4 \\ &= 100.05 \times 18/4 \\ &= 450.23 \text{ kNm} \end{aligned}$$

and for allowable value

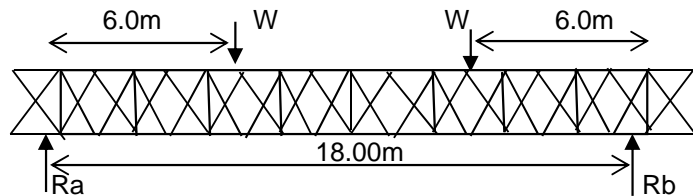
$$\begin{aligned} \text{allowable max moment} &= 450.23/1.50 \\ &= 300.15 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>450.23 kNm</b>
	<b>Allowable</b>	<b>300.15 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	18m X-Beam Load Combination 3			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

**Load Comb. 3**      PL at third points      10kN load applied at each of the two third points

Element	Action	Formula	Ultimate	Calculated	Factor	
Boom	Moment	$M_{c,Rd}$	16.60	0.83	20.05	
	Shear	$V_{Rd}$	143.12	2.05	69.68	
	Tension	$N_{o,Rd}$	471.94	21.78	21.67	
	Compression	$N_{b,Rd}$	470.25	67.91	6.92	
	Deflection	$d$		180.00	12.89	13.96
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	5.46
Vertical	Moment	$M_{c,Rd}$	0.87	0.03	27.12	
	Shear	$V_{Rd}$	22.67	0.05	503.87	
	Tension	$N_{o,Rd}$	86.77	0.79	109.83	
	Compression	$N_{b,Rd}$	84.30	4.67	18.04	
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	11.76
Diagonal	Tension	$N_{o,Rd}$	83.06	9.61	8.64	
	Compression	$N_{b,Rd}$	82.23	10.59	7.76	
<b>Factor</b>					<b>5.46</b>	



$$\text{Max Moment} = \frac{WL}{3}$$

so for ultimate condition

$$W = \frac{1.50 \times 10}{15.00} \text{ kN}$$

apply factor from above

$$W_f = 15.00 \times 5.46 = 81.90 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= \frac{W_f \times L}{3} \\ &= \frac{(81.90 \times 18)}{3} \\ &= 491.40 \text{ kNm} \end{aligned}$$

and for allowable value

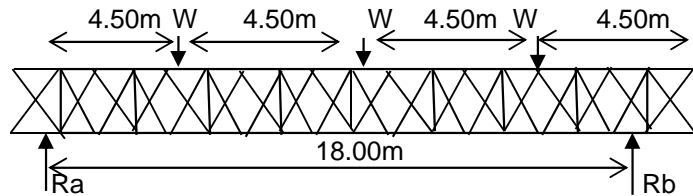
$$\begin{aligned} \text{allowable max moment} &= \frac{491.40}{1.50} \\ &= 327.60 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>491.40 kNm</b>
	<b>Allowable</b>	<b>327.60 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	18m X-Beam Load Combination 4			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

**Load Comb. 4** Load at quarter points  
10kN load applied at each of the three quarter points

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	1.14	14.60
	Shear	$V_{Rd}$	143.12	2.89	49.52
	Tension	$N_{o,Rd}$	471.94	35.02	13.48
	Compression	$N_{b,Rd}$	470.25	94.88	4.96
	Deflection	$d$	180.00	17.50	10.29
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	3.92
Vertical	Moment	$M_{c,Rd}$	0.87	0.05	18.86
	Shear	$V_{Rd}$	22.67	0.06	354.28
	Tension	$N_{o,Rd}$	86.77	0.93	93.30
	Compression	$N_{b,Rd}$	84.30	6.61	12.75
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	8.26
Diagonal	Tension	$N_{o,Rd}$	83.06	13.60	6.11
	Compression	$N_{b,Rd}$	82.23	14.99	5.49
<b>Factor</b>					<b>3.92</b>



$$\text{Max Moment} = WL/2$$

so for ultimate condition

$$W = \frac{1.50 \times 10}{15.00} \text{ kN}$$

apply factor from above

$$W_f = 15.00 \times 3.92 = 58.80 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= W_f \times L/2 \\ &= (58.80 \times 18)/2 \\ &= 529.20 \text{ kNm} \end{aligned}$$

and for allowable value

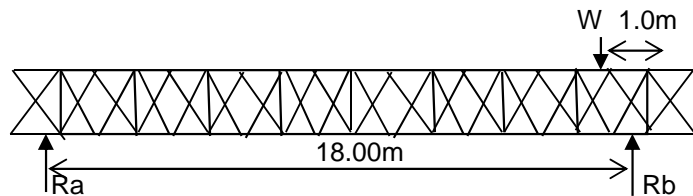
$$\begin{aligned} \text{allowable max moment} &= 529.20/1.50 \\ &= 352.80 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>529.20 kNm</b>
	<b>Allowable</b>	<b>352.80 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	18m X-beam Load Combination 5			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

**Load Comb. 5**      End Shear      10kN load applied at a 1.0m distance from the support

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	0.76	21.84
	Shear	$V_{Rd}$	143.12	2.21	64.79
	Tension	$N_{o,Rd}$	471.94	4.08	115.67
	Compression	$N_{b,Rd}$	470.25	15.19	30.96
	Deflection	$d$	180.00	2.76	65.22
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	14.11
Vertical	Moment	$M_{c,Rd}$	0.87	0.02	51.04
	Shear	$V_{Rd}$	22.67	0.02	944.75
	Tension	$N_{o,Rd}$	86.77	0.27	321.36
	Compression	$N_{b,Rd}$	84.30	4.45	18.96
	Combined Axial	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	14.70
Diagonal	Tension	$N_{o,Rd}$	83.06	7.09	11.72
	Compression	$N_{b,Rd}$	82.23	9.75	8.43
<b>Factor</b>					<b>8.43</b>



$$\text{Max Shear } R_b = W * 17 / 18$$

so for ultimate condition

$$W = \frac{1.50 * 10.0}{15.00} \text{ kN}$$

apply factor from above

$$W_f = 15.00 * 8.43 = 126.45 \text{ kN}$$

so maximum shear is as above

$$\begin{aligned} \text{Ultimate } Q_u &= W_f * 17 / 18 \\ &= (126.45 * 17) / 18 \\ &= 119.43 \text{ kN} \end{aligned}$$

and for allowable value

$$\begin{aligned} \text{allowable max shear} &= 119.43 / 1.50 \\ &= 79.62 \text{ kN} \end{aligned}$$

<b>Shear values</b>	<b>Ultimate</b>	<b>119.43 kN</b>
	<b>Allowable</b>	<b>79.62 kN</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	18m X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked: mmr	Date: Dec 16



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18.0m X-BEAM		
Loadcase	Ultimate	Allowable
No.	Moment	Moment
1 UDL	546.75	364.50
2 Point	450.23	300.15
3 Third	491.40	327.60
4 Quarter	529.20	352.80

Loadcase	Ultimate	Allowable
No.	Shear	Shear
5 End Shear	119.43	79.62

**Max Allowable Moment = 300.00 kNm**


**Max Allowable Shear = 79.50 kN**

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	24m X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked: mmr	Date: Dec 16



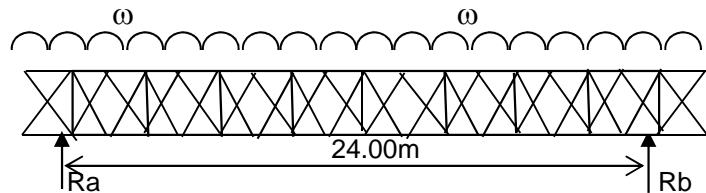
ALAN WHITE DESIGN

# 24m X-Beam Results

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	24m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 1**      UDL load      10kN/m applied along beam

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	7.91	2.10
	Shear	$V_{Rd}$	143.12	20.15	7.10
	Tension	$N_{o,Rd}$	471.94	240.51	1.96
	Compression	$N_{b,Rd}$	470.25	722.81	0.65
	Deflection	d	240.00	213.85	1.12
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	0.52
Vertical	Moment	$M_{c,Rd}$	0.87	0.29	2.96
	Shear	$V_{Rd}$	22.67	0.41	55.03
	Tension	$N_{o,Rd}$	86.77	5.19	16.72
	Compression	$N_{b,Rd}$	84.30	47.92	1.76
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	1.19
Diagonal	Tension	$N_{o,Rd}$	83.06	87.60	0.95
	Compression	$N_{b,Rd}$	82.23	104.38	0.79
			<b>Factor</b>		<b>0.52</b>



$$\text{Max Moment} = WL^2/8$$

so for ultimate condition

$$W = 1.5 \times 10 = 15.00 \text{ kN}$$

apply factor from above

$$Wf = 15 \times 0.52 = 7.80 \text{ kN}$$

so maximum moment is as above


$$\begin{aligned} \text{Ultimate } M_u &= Wf \times 24^2 / 8 \\ &= (7.80 \times 24^2) / 8 \\ &= 561.60 \text{ kNm} \end{aligned}$$

and for allowable value

$$\begin{aligned} \text{allowable max moment} &= 561.60 / 1.50 \\ &= 374.40 \text{ kNm} \end{aligned}$$

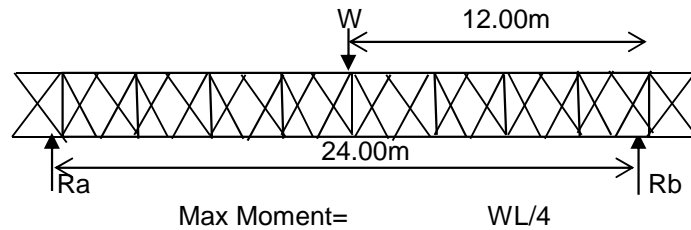
<b>Moment values</b>	<b>Ultimate</b>	<b>561.60 kNm</b>
	<b>Allowable</b>	<b>374.40 kNm</b>



CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	24m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 2**      Point load      10kN load applied at midspan of beam

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	0.86	19.30
	Shear	$V_{Rd}$	143.12	1.97	72.65
	Tension	$N_{o,Rd}$	471.94	35.55	13.28
	Compression	$N_{b,Rd}$	470.25	75.67	6.21
	Deflection	d	240.00	20.62	11.64
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	4.98
Vertical	Moment	$M_{c,Rd}$	0.87	0.02	43.38
	Shear	$V_{Rd}$	22.67	0.03	781.87
	Tension	$N_{o,Rd}$	86.77	0.75	115.69
	Compression	$N_{b,Rd}$	84.30	2.96	28.51
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	18.66
Diagonal	Tension	$N_{o,Rd}$	83.06	6.10	13.62
	Compression	$N_{b,Rd}$	82.23	6.85	12.01
<b>Factor</b>					<b>4.98</b>



so for ultimate condition

$$W = 1.50 \times 10 = 15.00 \text{ kN}$$

apply factor from above

$$W_f = 15 \times 4.98 = 74.70 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= W_f \times 24/4 \\ &= 74.70 \times 24/4 \\ &= 448.20 \text{ kNm} \end{aligned}$$

and for allowable value

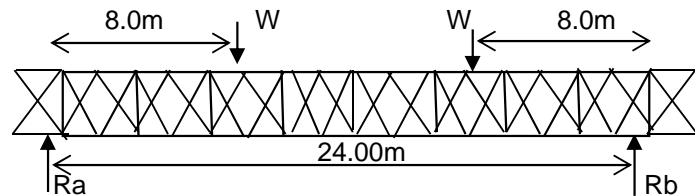
$$\begin{aligned} \text{allowable max moment} &= 448.20/1.50 \\ &= 298.80 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>448.20 kNm</b>
	<b>Allowable</b>	<b>298.80 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	24m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 3**      PL at third points      10kN load applied at each of the two third points

Element	Action	Formula	Ultimate	Calculated	Factor	
Boom	Moment	$M_{c,Rd}$	16.60	0.87	19.19	
	Shear	$V_{Rd}$	143.12	2.18	65.56	
	Tension	$N_{o,Rd}$	471.94	31.62	14.93	
	Compression	$N_{b,Rd}$	470.25	96.87	4.85	
	Deflection	$d$		240.00	29.44	8.15
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	4.07
Vertical	Moment	$M_{c,Rd}$	0.87	0.03	25.52	
	Shear	$V_{Rd}$	22.67	0.05	472.38	
	Tension	$N_{o,Rd}$	86.77	0.93	93.30	
	Compression	$N_{b,Rd}$	84.30	4.89	17.26	
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	11.18
Diagonal	Tension	$N_{o,Rd}$	83.06	10.15	8.18	
	Compression	$N_{b,Rd}$	82.23	11.29	7.28	
<b>Factor</b>					<b>4.07</b>	



$$\text{Max Moment} = \quad \quad \quad WL/3$$

so for ultimate condition

$$W = \quad \quad \quad 1.50 \times 10 \\ \quad \quad \quad \quad \quad \quad 15.00 \text{ kN}$$

apply factor from above

$$W_f = \quad \quad \quad 15.00 \times 4.07 \\ = \quad \quad \quad 61.05 \text{ kN}$$


so maximum moment is as above

$$\text{Ultimate } M_u = \quad \quad \quad W_f \times L/3 \\ = \quad \quad \quad (61.05 \times 24)/3 \\ = \quad \quad \quad 488.40 \text{ kNm}$$

and for allowable value

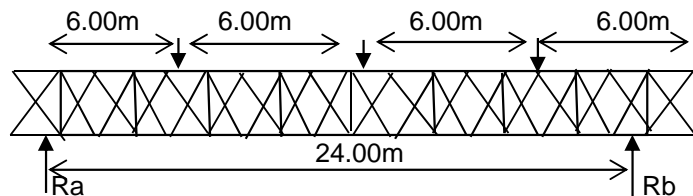
$$\text{allowable max moment} = \quad \quad \quad 488.40/1.50 \\ = \quad \quad \quad 325.60 \text{ kNm}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>488.40 kNm</b>
	<b>Allowable</b>	<b>325.60 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	24m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 4** Load at quarter points  
10kN load applied at each of the three quarter points

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	1.20	13.81
	Shear	$V_{Rd}$	143.12	3.03	47.31
	Tension	$N_{o,Rd}$	471.94	52.29	9.03
	Compression	$N_{b,Rd}$	470.25	139.89	3.36
	Deflection	$d$	240.00	40.81	5.88
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	2.83
Vertical	Moment	$M_{c,Rd}$	0.87	0.05	18.08
	Shear	$V_{Rd}$	22.67	0.07	338.42
	Tension	$N_{o,Rd}$	86.77	1.84	47.16
	Compression	$N_{b,Rd}$	84.30	6.75	12.49
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	8.03
Diagonal	Tension	$N_{o,Rd}$	83.06	14.19	5.85
	Compression	$N_{b,Rd}$	82.23	14.73	5.58
<b>Factor</b>					<b>2.83</b>



$$\text{Max Moment} = WL/2$$

so for ultimate condition

$$W = 1.50 * 10 = 15.00 \text{ kN}$$

apply factor from above

$$Wf = 15.00 * 2.83 = 42.45 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } Mu &= Wf * L / 2 \\ &= (42.45 * 24) / 2 \\ &= 509.40 \text{ kNm} \end{aligned}$$

and for allowable value

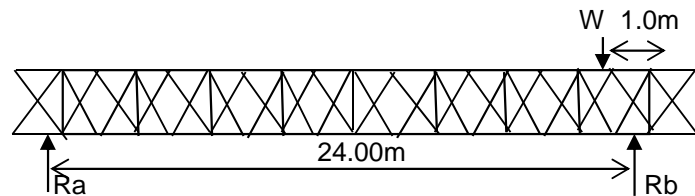
$$\begin{aligned} \text{allowable max moment} &= 509.40 / 1.50 \\ &= 339.60 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>509.40 kNm</b>
	<b>Allowable</b>	<b>339.60 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	24m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 5**      End Shear      10kN load applied at a 1.0m distance from the support

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	0.82	20.27
	Shear	$V_{Rd}$	143.12	2.35	60.80
	Tension	$N_{o,Rd}$	471.94	6.12	77.12
	Compression	$N_{b,Rd}$	470.25	22.39	21.00
	Deflection	d	240.00	6.59	36.42
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{Rd,x})^{1.7}]^{0.6} < 1.0$		1.00	11.32
Vertical	Moment	$M_{c,Rd}$	0.87	0.02	45.67
	Shear	$V_{Rd}$	22.67	0.03	839.78
	Tension	$N_{o,Rd}$	86.77	0.32	271.15
	Compression	$N_{b,Rd}$	84.30	4.77	17.68
	Combined Axial	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{Rd,x})^{1.7}]^{0.6} < 1.0$		1.00	13.58
Diagonal	Tension	$N_{o,Rd}$	83.06	7.78	10.68
	Compression	$N_{b,Rd}$	82.23	10.52	7.82
<b>Factor</b>					<b>7.82</b>



$$\text{Max Shear } R_b = W * 23 / 24$$

so for ultimate condition

$$W = \frac{1.50 * 10.0}{15.00} \text{ kN}$$

apply factor from above

$$W_f = 15.00 * 7.82 = 117.30 \text{ kN}$$

so maximum shear is as above

$$\begin{aligned} \text{Ultimate } Q_u &= W_f * 23 / 24 \\ &= (117.30 * 23) / 24 \\ &= 112.41 \text{ kN} \end{aligned}$$

and for allowable value

$$\begin{aligned} \text{allowable max shear} &= 112.41 / 1.50 \\ &= 74.94 \text{ kN} \end{aligned}$$

<b>Shear values</b>	<b>Ultimate</b>	<b>112.41 kN</b>
	<b>Allowable</b>	<b>74.94 kN</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	24m X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked: mmr	Date: Dec 16



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24.0m X-BEAM		
Loadcase	Ultimate	Allowable
No.	Moment	Moment
1 UDL	561.60	374.40
2 Point	448.20	298.80
3 Third	488.40	325.60
4 Quarter	509.40	339.60

Loadcase	Ultimate	Allowable
No.	Shear	Shear
5 End Shear	112.41	74.94

**Max Allowable Moment = 298.50 kNm**


**Max Allowable Shear = 74.50 kN**

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	36m X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked: mmr	Date: Dec 16



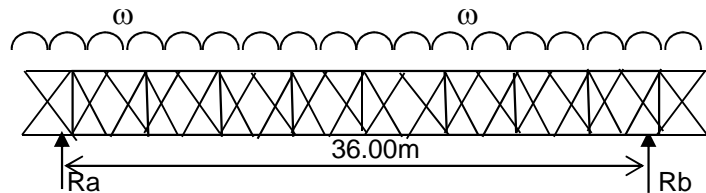
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# 36m X-Beam Results

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	36m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 1**      UDL load      10kN/m applied along beam

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	12.30	1.35
	Shear	$V_{Rd}$	143.12	30.70	4.66
	Tension	$N_{o,Rd}$	471.94	558.01	0.85
	Compression	$N_{b,Rd}$	470.25	1,675.75	0.28
	Deflection	d	300.00	1,034.00	0.29
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	0.24
Vertical	Moment	$M_{c,Rd}$	0.87	0.46	1.88
	Shear	$V_{Rd}$	22.67	0.65	35.05
	Tension	$N_{o,Rd}$	86.77	12.00	7.23
	Compression	$N_{b,Rd}$	84.30	69.36	1.22
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	0.80
Diagonal	Tension	$N_{o,Rd}$	83.06	136.73	0.61
	Compression	$N_{b,Rd}$	82.23	160.43	0.51
			<b>Factor</b>		<b>0.24</b>



$$\text{Max Moment} = WL^2/8$$

so for ultimate condition

$$W = 1.5 \times 10 = 15.00 \text{ kN}$$

apply factor from above

$$Wf = 15 \times 0.24 = 3.60 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= Wf \times 36^2 / 8 \\ &= (3.60 \times 36^2) / 8 \\ &= 583.20 \text{ kNm} \end{aligned}$$

and for allowable value

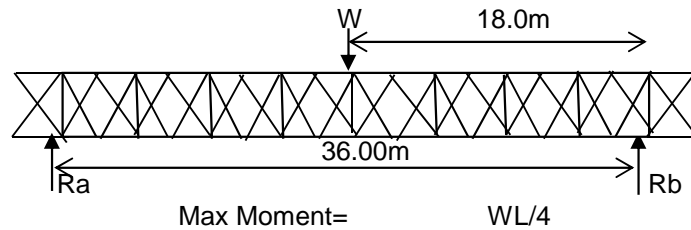
$$\begin{aligned} \text{allowable max moment} &= 583.20 / 1.50 \\ &= 388.80 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>583.20 kNm</b>
	<b>Allowable</b>	<b>388.80 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	36m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 2**      Point load      10kN load applied at midspan of beam

Element	Action	Formula	Ultimate	Calculated	Factor	
Boom	Moment	$M_{c,Rd}$	16.60	0.89	18.65	
	Shear	$V_{Rd}$	143.12	1.90	75.33	
	Tension	$N_{o,Rd}$	471.94	58.91	8.01	
	Compression	$N_{b,Rd}$	470.25	129.00	3.65	
	Deflection	$d$		300.00	72.70	4.13
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	3.18
Vertical	Moment	$M_{c,Rd}$	0.87	0.02	36.15	
	Shear	$V_{Rd}$	22.67	0.03	666.89	
	Tension	$N_{o,Rd}$	86.77	1.03	84.24	
	Compression	$N_{b,Rd}$	84.30	3.36	25.06	
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	16.09
Diagonal	Tension	$N_{o,Rd}$	83.06	7.18	11.57	
	Compression	$N_{b,Rd}$	82.23	8.20	10.02	
<b>Factor</b>					<b>3.18</b>	



so for ultimate condition

$$W = 1.50 \times 10 = 15.00 \text{ kN}$$

apply factor from above

$$W_f = 15 \times 3.18 = 47.70 \text{ kN}$$

so maximum moment is as above


$$\begin{aligned} \text{Ultimate } M_u &= W_f \times 36/4 \\ &= 47.70 \times 36/4 \\ &= 429.30 \text{ kNm} \end{aligned}$$

and for allowable value

$$\begin{aligned} \text{allowable max moment} &= 429.30/1.50 \\ &= 286.20 \text{ kNm} \end{aligned}$$

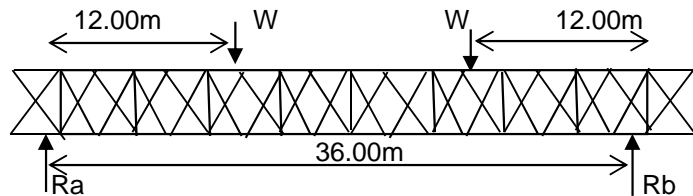
<b>Moment values</b>	<b>Ultimate</b>	<b>429.30 kNm</b>
	<b>Allowable</b>	<b>286.20 kNm</b>



CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	36m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 3** PL at third points 10kN load applied at each of the two third points

Element	Action	Formula	Ultimate	Calculated	Factor	
Boom	Moment	$M_{c,Rd}$	16.60	0.99	16.82	
	Shear	$V_{Rd}$	143.12	2.44	58.59	
	Tension	$N_{o,Rd}$	471.94	53.20	8.87	
	Compression	$N_{b,Rd}$	470.25	161.58	2.91	
	Deflection	d		300.00	102.48	2.93
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	2.57
Vertical	Moment	$M_{c,Rd}$	0.87	0.04	22.83	
	Shear	$V_{Rd}$	22.67	0.05	427.81	
	Tension	$N_{o,Rd}$	86.77	1.35	64.27	
	Compression	$N_{b,Rd}$	84.30	5.19	16.23	
	Combined		$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	10.32
Diagonal	Tension	$N_{o,Rd}$	83.06	11.23	7.40	
	Compression	$N_{b,Rd}$	82.23	12.70	6.48	
<b>Factor</b>					<b>2.57</b>	



$$\text{Max Moment} = WL/3$$

so for ultimate condition

$$W = \frac{1.50 \times 10}{15.00} \text{ kN}$$

apply factor from above

$$W_f = \frac{15.00 \times 2.57}{1} = 38.55 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= W_f \times L/3 \\ &= (38.55 \times 36)/3 \\ &= 462.60 \text{ kNm} \end{aligned}$$

and for allowable value

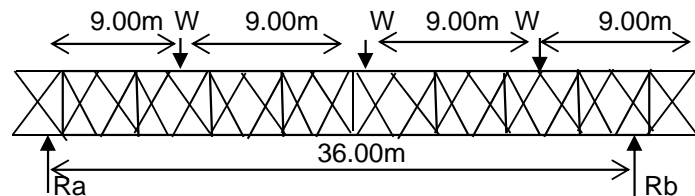
$$\begin{aligned} \text{allowable max moment} &= \frac{462.60}{1.50} \\ &= 308.40 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>462.60 kNm</b>
	<b>Allowable</b>	<b>308.40 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	36m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmm	Date: Dec 16	

**Load Comb. 4** Load at quarter points  
10kN load applied at each of the three quarter points

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	1.33	12.46
	Shear	$V_{Rd}$	143.12	3.29	43.46
	Tension	$N_{o,Rd}$	471.94	83.64	5.64
	Compression	$N_{b,Rd}$	470.25	226.00	2.08
	Deflection	$d$	300.00	136.47	2.20
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	1.85
Vertical	Moment	$M_{c,Rd}$	0.87	0.05	16.69
	Shear	$V_{Rd}$	22.67	0.07	314.92
	Tension	$N_{o,Rd}$	86.77	1.65	52.59
	Compression	$N_{b,Rd}$	84.30	7.03	12.00
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	7.60
Diagonal	Tension	$N_{o,Rd}$	83.06	15.25	5.44
	Compression	$N_{b,Rd}$	82.23	17.19	4.78
<b>Factor</b>					<b>1.85</b>



$$\text{Max Moment} = WL/2$$

so for ultimate condition

$$W = \frac{1.50 \times 10}{15.00} \text{ kN}$$

apply factor from above

$$W_f = 15.00 \times 1.85 = 27.75 \text{ kN}$$


so maximum moment is as above

$$\begin{aligned} \text{Ultimate } M_u &= W_f \times L/2 \\ &= (27.75 \times 36)/2 \\ &= 499.50 \text{ kNm} \end{aligned}$$

and for allowable value

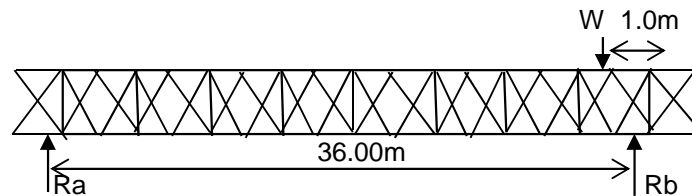
$$\begin{aligned} \text{allowable max moment} &= 499.50/1.50 \\ &= 333.00 \text{ kNm} \end{aligned}$$

<b>Moment values</b>	<b>Ultimate</b>	<b>499.50 kNm</b>
	<b>Allowable</b>	<b>333.00 kNm</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	36m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

**Load Comb. 5**      End Shear      10kN load applied at a 1.0m distance from the support

Element	Action	Formula	Ultimate	Calculated	Factor
Boom	Moment	$M_{c,Rd}$	16.60	0.93	17.87
	Shear	$V_{Rd}$	143.12	2.62	54.61
	Tension	$N_{o,Rd}$	471.94	13.16	35.86
	Compression	$N_{b,Rd}$	470.25	44.06	10.67
	Deflection	d	300.00	27.19	11.03
	Combined	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	7.23
Vertical	Moment	$M_{c,Rd}$	0.87	0.02	36.15
	Shear	$V_{Rd}$	22.67	0.03	687.09
	Tension	$N_{o,Rd}$	86.77	0.46	188.63
	Compression	$N_{b,Rd}$	84.30	5.23	16.12
	Combined Axial	$(N_{ed}/N_{Rd})^{1.3} + [(M_{ed,x}/M_{rd,x})^{1.7}]^{0.6} < 1.0$		1.00	11.94
Diagonal	Tension	$N_{o,Rd}$	83.06	9.03	9.20
	Compression	$N_{b,Rd}$	82.23	11.94	6.89
<b>Factor</b>					<b>6.89</b>



$$\text{Max Shear } R_b = W * 29/30$$

so for ultimate condition

$$W = \frac{1.50 * 10.0}{15.00} \text{ kN}$$

apply factor from above

$$W_f = 15.00 * 6.89 = 103.35 \text{ kN}$$


so maximum shear is as above

$$\begin{aligned} \text{Ultimate } Q_u &= W_f * 35/36 \\ &= (103.35 * 35)/36 \\ &= 100.48 \text{ kN} \end{aligned}$$

and for allowable value

$$\begin{aligned} \text{allowable max shear} &= 100.48/1.50 \\ &= 66.99 \text{ kN} \end{aligned}$$

<b>Shear values</b>	<b>Ultimate</b>	<b>100.48 kN</b>
	<b>Allowable</b>	<b>66.99 kN</b>

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016			 ALAN WHITE DESIGN
	Element :	36m X-Beam Results			
	Job Number :	W0224	By : mrb	Date: Dec 16	
	Document No :	001A	Checked: mmr	Date: Dec 16	

<b>36.0m X-BEAM</b>		
Loadcase	Ultimate	Allowable
No.	Moment	Moment
1 UDL	583.20	388.80
2 Point	429.30	286.20
3 Third	462.60	308.40
4 Quarter	499.50	333.00

Loadcase	Ultimate	Allowable
No.	Shear	Shear
5 End Shear	100.48	66.99

**Max Allowable Moment = 286.00 kNm**

**Max Allowable Shear = 70.00 kN**

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	Overall X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked: mmr	Date: Dec 16



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## Overall X-Beam Results

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked :mmr	Date: Dec 16



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**Load case 1 : UDL**

<b>1.5m X-BEAM</b>	
<b>Loadcase 1</b>	<b>Ultimate Moment</b>
<b>Length (m)</b>	
12	448.20
18	546.75
24	561.60
36	583.20

Average 534.94 kNm  
 Minimum 448.20 kNm

**Load case 2 : Central Point Load**

<b>1.5m X-BEAM</b>	
<b>Loadcase 2</b>	<b>Ultimate Moment</b>
<b>Length (m)</b>	
12	431.10
18	450.23
24	448.20
36	429.30

Average 440.66 kNm  
 Minimum 431.10 kNm

**Load case 3 : Two Point Loads at Third Points**

<b>1.5m X-BEAM</b>	
<b>Loadcase 3</b>	<b>Ultimate Moment</b>
<b>Length (m)</b>	
12	476.40
18	491.40
24	488.40
36	462.60

Average 483.90 kNm  
 Minimum 476.40 kNm

CALCULATION SHEET	Project :	Apollo 1.5m X-beam 2016		
	Element :	X-Beam Results		
	Job Number :	W0224	By : mrb	Date: Dec 16
	Document No :	001A	Checked :mmr	Date: Dec 16



**Load case 4 : Three Point Loads at Quarter Points**

<b>1.5m X-BEAM</b>	
<b>Loadcase 4</b>	<b>Ultimate Moment</b>
<b>Length (m)</b>	
12	513.90
18	529.20
24	509.40
36	499.50

Average 521.55 kNm  
 Minimum 513.90 kNm

**Load case 5 : Shear**

<b>1.5m X-BEAM</b>	
<b>Loadcase 5</b>	<b>Ultimate Shear</b>
<b>Length (m)</b>	
12	146.03
18	119.43
24	112.41
36	100.48

Average 132.73 kN  
 Minimum 119.43 kN

## Overall Graded Results for Allowable Working Loads on a 1.5m X-Beam

For simply supported Apollo1.5m X-BEAM with a compression chord restraint at 1.0m intervals

### Test Results

	Span (m)			
	12	18	24	36
Allowable Moment	287.4	300.0	298.5	286.0
Allowable Shear (Load on Vertical)	97.0	79.5	74.5	67.0



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### Allowable loads for load distributions from results

Type of Load	Clear span (m)	Span (m)			
		12	18	24	36
Uniformly Distributed load	kN/m	16.0	7.4	4.1	1.8
Total UDL	kN	191.6	133.3	99.5	63.6
Single point load (mid Point)	kN	95.8	66.7	49.8	31.8
Two point loads (third points)	Each kN	71.9	50.0	37.3	23.8
Three point loads (quarter points)	Each kN	47.9	33.3	24.9	15.9

### Extrapolated Allowable loads for load distributions

Type of Load	Clear span (m)	Clear span (m)																	
		11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	
Uniformly Distributed load	kN/m	17.6	16.0	13.6	11.7	10.2	9.0	8.0	7.4	6.6	6.0	5.4	4.9	4.5	4.1	3.7	3.4	3.1	
Total UDL	kN	194.0	191.6	176.9	164.2	153.3	143.8	135.3	133.3	125.7	119.4	113.7	108.5	103.8	99.5	91.5	88.0	84.7	
Single point load (mid Point)	kN	104.5	95.8	88.5	82.1	76.7	71.9	67.6	66.7	62.8	59.7	56.9	54.3	51.9	49.8	45.8	44.0	42.4	
Two point loads (third points)	Each kN	78.4	71.9	66.3	61.6	57.5	53.9	50.7	50.0	47.1	44.8	42.6	40.7	38.9	37.3	34.3	33	31.8	
Three point loads (quarter points)	Each kN	52.3	47.9	44.2	41.1	38.3	35.9	33.8	33.3	31.4	29.9	28.4	27.1	26.0	24.9	22.9	22	21.2	
Type of Load	Clear span (m)																		
		28	29	30	31	32	33	34	35	36									
Uniformly Distributed load	kN/m	2.9	2.7	2.5	2.4	2.2	2.1	2.0	1.9	2									
Total UDL	kN	81.7	78.9	76.3	73.8	71.5	69.3	67.3	65.4	64									
Single point load (mid Point)	kN	40.9	39.4	38.1	36.9	35.8	34.7	33.6	32.7	32									
Two point loads (third points)	Each kN	30.6	29.6	28.6	27.7	26.8	26.0	25.2	24.5	24									
Three point loads (quarter points)	Each kN	20.4	19.7	19.1	18.5	17.9	17.3	16.8	16.3	16									



- Notes:
1. This table is provided as a guide only and assume all loads are applied at nodes. All scaffolds and structures should be checked by a qualified structural engineer.
  2. Maximum capacity of a point load mid way between nodes is 15kN but overall buckling of the top chord should be checked if loads are placed other than at restrained nodes. Compression chord restraint required at 1.0m c/c
  3. Factor of Safety = 1.65 ( = 1.5\*1.1 (material factor))
  4. Calculations as per BS EN 1999-1-1
  5. For design purposes the allowable bending moment is 282.50kNm and the allowable shear is 66.50kN.

Graph Summary of Allowable Working Loads for a 1.5m X-Beam to BS EN 1999-1-1



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